

CH301H – Principles of Chemistry I: Honors
 Fall 2013, Unique 52195

Quiz 3, October 3, 2013

B^{4+} is a one-electron atom and therefore certain properties can be explained by the Bohr Model:

$$r_n = \frac{\epsilon_0 n^2 h^2}{\pi Z e^2 m_e} \quad E_n = -\frac{Z^2 e^4 m_e}{8 \epsilon_0^2 n^2 h^2}$$

- Estimate the ionization energy of the remaining electron in B^{4+} .
- An electron with $n = 7$ moves to $n = 6$. Is light emitted from or absorbed by the atom?
- What is the wavelength of the photon that is either emitted or absorbed in part b)?
- What color would you observe if you were watching this transition?

The following information may be helpful.

$$\begin{aligned} q &= 1.602 \times 10^{-19} \text{ C} \\ \epsilon_0 &= 8.854 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1} \\ h &= 6.626 \times 10^{-34} \text{ J s} \\ c &= 3.0 \times 10^8 \text{ m s}^{-1} \\ m_e &= 9.11 \times 10^{-31} \text{ kg} \end{aligned}$$

$$E_n = -\frac{Z^2 e^4 m_e}{8 \epsilon_0^2 n^2 h^2}$$

$$\begin{aligned} \text{a) IE} &= E(n=\infty) - E(n=1) = -\frac{Z^2 e^4 m_e}{8 \epsilon_0^2 (1)^2 h^2} \\ &= 0 - \left(-2.18 \times 10^{-18} \text{ J} \right) \times \frac{25}{1} = 5.45 \times 10^{-17} \text{ J (for 1 atom)} \\ \text{IE (1 mol)} &= 5.45 \times 10^{-17} \frac{\text{J}}{\text{atom}} \left| \frac{6.023 \times 10^{23} \text{ atoms}}{1 \text{ mol}} \right. = \boxed{3.28 \times 10^7 \text{ J/mol}} \end{aligned}$$

b) Emission

$$\begin{aligned} \text{c) transition } n=7 \rightarrow n=6 \\ \Delta E &= E(n=6) - E(n=7) \\ &= -\frac{(2.18 \times 10^{-18} \text{ J})(25)}{36} \\ \Delta E &= -4.01644 \times 10^{-19} \text{ J} \end{aligned}$$

$$\begin{aligned} \Delta E = h\nu = \frac{hc}{\lambda} \Rightarrow \lambda = \frac{hc}{\Delta E} \\ \lambda = \frac{6.626 \times 10^{-34} \text{ J s} \times 3 \times 10^8 \text{ m/s}}{4.01644 \times 10^{-19} \text{ J}} \\ \lambda = 4.949 \times 10^{-7} \text{ m} \\ \lambda = \boxed{495 \text{ nm}} \\ \text{d) blue/green} \end{aligned}$$